



ENERGY STAR® Connected Thermostat Products

Method to Demonstrate Field Savings Version 1.0 (rev. Dec-2016)

1) OVERVIEW

This method shall be used to demonstrate field savings for ENERGY STAR Connected Thermostat (CT) Products.

2) APPLICABILITY

This ENERGY STAR Method is applicable to Connected Thermostat Products as defined in the ENERGY STAR Eligibility Criteria for Connected Thermostat Products.

3) DEFINITIONS

Unless otherwise specified, all terms used in this document are consistent with the definitions contained in the ENERGY STAR Eligibility Criteria for Connected Thermostat Products.

4) DEMONSTRATING FIELD SAVINGS

Field savings of CT Products shall be assessed for product certification as well as for periodic reporting as detailed in the Partner Commitments section of the ENERGY STAR Program Requirements for Connected Thermostat Products.

1. Install and configure the **most recent release** of the ENERGY STAR CT Field Savings Software using the open source code and instructions available at:

- Documentation: <http://thermostat.readthedocs.org/en/latest/>
- Source code: <https://github.com/impactlab/thermostat>

2. From the set of all instances of a fielded CT Product Family in the US, generate a randomly selected data set via the following procedure:

a. Generate a metadata file that includes all instances of a fielded CT Product in the US, with the following information:

- i. included data: "thermostat_id", "equipment_type", "zipcode", "date1", "date2";
- ii. thermostat_id is a unique alphanumeric string;

Important Note: thermostat_id shall be a preexisting unique identifier associated with the CT Device (e.g. MAC address or serial number) or directly mapped from it using consistent rules (e.g. to remove non alphanumeric characters or to eliminate duplicates).

iii. equipment_type:

- 0: Other – e.g. multi-zone multi-stage, modulating, dual fuel. Note: module will not output savings data for this type
- 1: Single stage heat pump with electric resistance aux and/or emergency heat (i.e. strip heat)
- 2: Single stage heat pump without additional and/or supplemental heating sources
- 3: Single stage non heat pump with single-stage central air conditioning
- 4: Single stage non heat pump without central air conditioning
- 5: Single stage central air conditioning without central heating;

- iv. zipcode is the US ZIP code where the thermostat is installed;
- v. date1 is the first date for which interval data was reported; and
- vi. date2 is the last date for which interval data was reported.

- b. from the above metadata file, generate a new metadata file that eliminates CTs according to the following rules:
 - i. thermostat_id is null or invalid;
 - ii. equipment_type = 0, or changes during the reporting period;
 - iii. zipcode is null, invalid, or changes during the reporting period;
 - iv. date1 is after the reporting period start date; and
 - v. date2 is before the reporting period stop date.
 - c. from the above metadata file, split CTs into 5 climate zone metadata files, using [this file](#), which maps U.S. ZIP codes with the following Energy Information Administration (EIA) climate zones:
 - Cold/Very Cold
 - Hot Dry/Mixed Dry
 - Hot Humid
 - Mixed Humid
 - Marine
 - d. using Python Natsort, sort each climate zone metadata file by the unique thermostat_id assigned to each thermostat.¹
 - e. using the Python Numpy random number generator, set a seed (supplied by EPA) for each climate zone manually with numpy.random.seed (number) and record these numbers.¹

Important Note: Seeds must be set manually and documented by Partner in order for sample to be reproducible and/or auditable. Additionally, using numpy.random.seed() without specifying a seed (empty parenthesis) is unable to be reconstructed, thus *should not* be used when submitting data.
 - f. for each of the five EIA climate zones, generate metadata files with 250 CTs using the Numpy function numpy.random.choice, using replace=False to prevent sampling duplicates. If the Partner has fewer than 250 thermostats in an EIA climate zone from which to sample, include all thermostats for that climate zone.¹
 - g. using the above metadata files, generate files that follow the requisite file format and content requirements in <http://thermostat.readthedocs.io/en/latest/tutorial.html#input-data>.¹
 - a single metadata file that includes all CTs from the above step; and
 - a separate interval data file for each included unique thermostat_id.
3. Verify that this data set:
 - a. consists of one metadata file and *n* interval data files (one interval data file for each CT in the sample);
 - b. includes CT Products in each of the five EIA climate zones: Very Cold/Cold, Hot Dry/Mixed Dry, Hot Humid, Mixed Humid, and Marine;
 - c. adheres to the relevant reporting period criteria as detailed in the Partner Commitments section of the ENERGY STAR Program Requirements for Connected Thermostat Products; and
 - d. includes only CT Products that control HVAC equipment types 1 thru 5 in 2.a.iii above.
 4. Process the data set using the ENERGY STAR CT Field Savings Software. The output includes:
 - Mean cooling and heating savings scores (% run time reduction) with associated standard error of the mean, and decile bins, in each of five EIA climate zones;
 - The lower 95% confidence interval of the mean cooling and heating savings scores (% run time reduction) with decile bins in each of the five EIA climate zones;

¹ see_Sample Code in Appendix A

- Weighted national average cooling and heating savings scores (% run time reduction) with associated standard error of the mean;
 - Weighted national average of the lower 95% confidence interval of the mean cooling and heating savings scores (% run time reduction);
 - Mean resistance heat utilization for heat pumps with backup electric resistance heating, in 5°F outdoor temperature bins from 60°F to 0°F across all climate zones.
5. Submit the CT Field Savings Software output file
 - a. to the Certification Body for initial product certification, or
 - b. to EPA for ongoing reporting.
 6. Retain the following data for a period not less than five years from the associated file submission:
 - a. raw data files for each thermostat_id in the CT data set used to assess savings;
 - b. all metadata files created in step 4.2. and all random seeds with a reference to the metadata files for which each seed was used
 - c. CT data set files, generated in step 4.2.g., and used with the ENERGY STAR CT Field Savings Software to assess reported savings; and
 - d. All output files submitted to EPA or to certification bodies.

APPENDIX A: CODE FOR SORTING AND REPRODUCIBLE RANDOM SAMPLING OF THERMOSTATS

```
import numpy as np
import pickle
#Package Notes, Natsort 5.0.1
from natsort import natsorted

#DEBUG: state caching
prng_state_exact = np.random.get_state()

#DEBUG: Save state via pickle
with open('prng_state.pickle','wb') as f:
    pickle.dump(prng_state_exact,f)

# #DEBUG: Code to load old state and set PRNG to that state
# with open('prng_state.pickle','rb') as f:
#     reload_state = pickle.load(f)
# np.random.set_state(reload_state)

#Load sample target data; Note if 0:n index replaced with data/thermostat id's,
will sample unique id's instead of indicies
EIAColdVCold = np.arange(500)
EIAHotHumid = np.arange(500)
EIAMixedHumid = np.arange(500)
EIAHDMD = np.arange(500)
EIAMarine = np.arange(500)

#Natural Sort Imported data by value
SampEIAColdVCold = natsorted(SampEIAColdVCold)
SampEIAHotHumid = natsorted(SampEIAHotHumid)
SampEIAMixedHumid = natsorted(SampEIAMixedHumid)
SampEIAHDMD = natsorted(SampEIAHDMD)
SampEIAMarine = natsorted(SampEIAMarine)

#Sample target data, applying 1 seed per climate zone
np.random.seed(101)
SampEIAColdVCold = np.random.choice(EIAColdVCold,250, replace=False )
np.random.seed(102)
SampEIAHotHumid = np.random.choice(EIAHotHumid,250, replace=False )
np.random.seed(103)
SampEIAMixedHumid = np.random.choice(EIAMixedHumid,250, replace=False )
np.random.seed(104)
SampEIAHDMD = np.random.choice(EIAHDMD,250, replace=False )
np.random.seed(105)
SampEIAMarine = np.random.choice(EIAMarine,250, replace=False )

#Sort Sampled data by value
SampEIAColdVCold = np.sort(SampEIAColdVCold)
SampEIAHotHumid = np.sort(SampEIAHotHumid)
SampEIAMixedHumid = np.sort(SampEIAMixedHumid)
SampEIAHDMD = np.sort(SampEIAHDMD)
SampEIAMarine = np.sort(SampEIAMarine)

#Create matrix for all samples, Matrix format best for indicies
SortedEIASample =
np.vstack((SampEIAColdVCold,SampEIAHotHumid,SampEIAMixedHumid,SampEIAHDMD,SampEIAMarine))

#Create long format output, best for vector of thermostat id's
```

```
results = SampEIAColdVCold
outfile =
np.append(results, [SampEIAHotHumid, SampEIAMixedHumid, SampEIAHDMD, SampEIAMarine])

#Save Sample items to file
np.savetxt('PRNG.csv', SortedEIASample, delimiter=",")
np.savetxt('PRNGvector.csv', outfile, delimiter=",")
```

APPENDIX B: DESCRIPTION OF SAVINGS METHODOLOGY & ALGORITHMS USED IN THE ENERGY STAR CT FIELD SAVINGS SOFTWARE

The software consists of documentation plus two modules which assess CT savings expressed as run time reduction relative to the baseline. This description pertains to the V1.0 release.

○ *Thermostat Module*

The thermostat module separately assesses HVAC heating and cooling savings attributed to a CT.

1. Input files consist of:
 - a metadata file that contains the unique ID, controlled HVAC type, ZIP code and interval data file name for each CT in the data set; and
 - an interval data file for each CT in the data set.
2. The module will not assess savings for CT data files that are missing too much data, or if corresponding outdoor temperature data is not available. Indoor and outdoor temperature data gaps of up to 2 hours are interpolated. Days with gaps longer than 2 hours are excluded from the analysis. If more than 5% of days are missing HVAC run time data, the CT is excluded.
3. The thermostat module output is a.csv file that includes a separate row for each CT in the data set. Columns in the output file include:
 - a. Unique CT ID;
 - b. Controlled HVAC type;
 - c. ZIP code in which the thermostat is installed;
 - d. Heating savings;
 - e. Cooling savings;
 - f. Resistance Heating Utilization; and
 - g. Associated statistical data.

○ *Statistics Module*

1. A thermostat module output file comprises the input to the statistics module.
2. The statistics module output is a .csv file that includes:
 - a. Regional heating and cooling savings as average savings of multiple instances of a CT model in each of the five EIA climate zones. The output file includes the climate zone, decile bins, means, and standard errors of the mean for all numerical outputs in the individual thermostat output files generated by the thermostat module. It also includes the lower 95% confidence limit for heating and cooling savings;
 - b. National heating and cooling savings assessed as a weighted average of regional savings. Weighting is by the proportion of national heating and cooling energy, respectively, used in each of the five EIA climate zones. The output file also includes the weighted average decile bins, weighted average standard error of the mean, and the lower 95% confidence limit of the weighted average; and
 - c. Resistance heat utilization (%) in 5°F bins from 0°F to 60°F (applicable to heating with heat pumps only)

Source code and detailed documentation are available at the following locations:

Documentation: <http://thermostat.readthedocs.org/en/latest/>

Source code: <https://github.com/impactlab/thermostat>

OVERVIEW OF SOFTWARE USAGE

Step 1 – Use the thermostat module to assess savings for n CTs that comprise a sample set.

1. *The module will assess Savings for CT1 as follows:*
 - a. *Develop Thermal/HVAC Model* – the software constructs a model of the relationship between heating and cooling HVAC run time, outside temperature, and temperature choices for the CT;
 - b. *Determine Baseline Comfort Temperatures* – the software parses the CT indoor temperature history to determine occupants' preferred temperatures for heating and cooling;
 - c. *Assess Baseline Run Times* – the software uses the thermal/HVAC model to assess baseline heating and cooling run times for the CT; i.e. what run times would have been under 24/7 use of baseline comfort temperatures;
 - d. *Assess CT Savings* – the software generates an output file that includes CT savings; expressed as percent run time reduction relative to the baseline. For heat pumps, the software also outputs Resistance Heat Utilization (RHU), the proportion of total heating run time that includes auxiliary and emergency heating.
2. *The module repeats for each of the remaining CTs in the sample set. Once evaluation of the sample set is complete, the output file will include n rows of data, one row for each of the n CTs in the sample set.*

Step 2 – Use the statistics module to assess aggregate national and regional savings

1. *Regional CT savings* – With a thermostat module output file serving as the input, the statistics module outputs average regional HVAC savings in the five EIA² climate zones, along with associated statistics.
2. *National CT savings* – the software also outputs national heating and cooling savings as a weighted average of regional savings, along with associated statistics. Regional savings are weighted by the proportion of national heating or cooling energy consumed in each of the five EIA climate zones.
3. *Resistance heating utilization (RHU)* – for heat pumps, the statistics module also outputs average regional and national RHU and associated statistics.

THERMOSTAT MODULE IMPLEMENTATION DETAIL

Common Terms and Calculations

- *Core Days*
 - Core heating days – days where daily heating run time \geq 30 minutes with no cooling, excluding days that exceed the missing data thresholds, as previously noted.
 - Core cooling days – days where daily cooling \geq 30 minutes with no heating, excluding days that exceed the missing data thresholds, as previously noted.

² https://www.eia.gov/consumption/residential/reports/images/climatezone_eere-lg.jpg

Note: Only primary heating source run times are assessed to determine core heating days. That is, auxiliary and emergency electric resistance heat run times associated with heat pumps are not included.

- **Baseline Assessment** – occupant’s preferred comfort temperatures for heating and cooling³:
 - Using data reported by the CT for core heating days, determine the preferred comfort temperature for heating:

T base heat (°F) = 90th percentile of indoor temperature history for core heating days.
Not a Number (NaN) values are ignored.
 - Using data reported by the CT for core cooling days, determine the preferred comfort temperature for cooling:

T base cool (°F) = 10th percentile of indoor temperature history for core cooling days.
NaN values are ignored.

Assess Heating Savings

- Develop the CT/home’s unique thermal/HVAC heating run time model
 - Calculate daily Heating Thermal Demand (*daily HTD_d*) for each core heating day in the interval data file:
 - Calculate the average hourly indoor minus outdoor temperature difference (*hourly ΔT_{d,n}*) for each core heating day:
 - Using the ZIP code included in the metadata file, determine the closest NOAA weather station that is in the same climate zone as the CT and look up hourly outdoor temperatures:

hourly outdoor T_{d,n} (°F), where
d is the core cooling day (*d* = 001, 002, 003 ... *x*),
n is the hour; (*n* = 01, 02, 03, ... 24)
 - *hourly ΔT_{d,n} (°F) = hourly indoor T_{d,n} – hourly outdoor T_{d,n}*, where
d is the core heating day (*d* = 001, 002, 003 ... *x*), and
n is the hour; (*n* = 01, 02, 03, ... 24).
 - Starting with an assumed value of zero for Tau (*τ_h* = 0), calculate the daily Heating Thermal Demand (*daily HTD_d*), as follows:

daily HTD_d (°F) = $\frac{\sum_{n=1}^{24} [hourly \Delta T_{d,n} - \tau_h]_+}{24}$, where
d is the core heating day (*d* = 001, 002, 003 ... *x*),
n is the hour; (*n* = 01, 02, 03, ... 24),
τ_h is the Δ*T* associated with *HTD* = 0 (zero heating run time), reflecting that homes with no heat running tend to be warmer than their surroundings, and
[]₊ indicates that the term is zero if its value would be negative
 - For the set of all core heating days in the CT interval data file, use ratio estimation to calculate *α_h*, the homes responsiveness to heating, which should be positive

α_h (minutes/°F) = RT actual heat / $\sum_{d=1}^x$ daily HTD_d, where
RT actual heat is the sum of heating run times for all core heating days in the CT interval data file.
 - For the set of all core heating days in the CT interval data file, optimize *τ_h* that results in

³ Methodology described in paragraph 3.1.2 of “[A DATA-DRIVEN FRAMEWORK FOR COMPARING RESIDENTIAL THERMOSTAT ENERGY PERFORMANCE](#),” Bryan Urban and Kurt Roth, Fraunhofer USA, July 2014.

minimization of the sum of squares of the difference between daily run times reported by the CT, and calculated daily heating run times. Next recalculate α_h (iaw the above step) and record the model's parameters (τ_h, α_h)⁴:

$\sum_{d=1}^x (\text{actual RT heat}_d - \text{daily RT heat}_d)^2$ is minimized, where

$$\text{daily RT heat}_d = \alpha_h * \text{daily HTD}_d$$

actual RT heat_d is the total daily heating run time reported by the CT for that core heating day

d is the core heating day ($d = 001, 002, 003 \dots x$)

Note that α_h characterizes the response of the home to heating and τ_h is the difference between inside and outside temperatures when heating run time = 0

- Calculate the cumulative baseline run time for the collection of all core heating days in the CT interval data file (i.e. what would have occurred over the set of all core heating days in the reporting period, had the home been held constant at the preferred heating comfort temperature).

- Calculate the baseline daily Heating Thermal Demand (*daily HTD base_d*) for each core heating day in the CT interval data file

- Calculate the difference between the occupant's preferred comfort temperature for heating and the average outside temperature for each hour of each core heating day (*hourly ΔT base heat_{d,n}*):

$$\text{hourly } \Delta T \text{ base heat}_{d,n} (\text{°F}) = T \text{ base heat} - \text{hourly outdoor } T_{d,n}, \text{ where}$$

d is the core heating day ($d = 001, 002, 003 \dots x$),

n is the hour ($n = 01, 02, 03, \dots 24$),

T base heat is the occupant's preferred comfort temperature for heating, and

hourly outdoor T_{d,n} is the average outdoor temperature for that hour reported by the nearest NOAA weather station in the same climate zone as the CT.

- Calculate baseline daily Heating Thermal Demand (*daily HTD base_d*)

$$\text{daily HTD base}_d = \frac{\sum_{n=1}^{24} |\text{hourly } \Delta T \text{ base heat}_{d,n} - \tau_h|_+}{24}, \text{ where}$$

d is the core heating day ($d = 001, 002, 003 \dots x$),

n is the hour ($n = 01, 02, 03, \dots 24$),

τ_h , determined above, is a constant that is part of CT/home's thermal/HVAC heating run time model, and

[]₊ indicates that the term is zero if its value would be negative.

- Calculate baseline run time as the sum of daily baseline run times for the set of core heating days in the CT interval data file

$$\text{RT base heat (minutes)} = \sum_{d=1}^x \alpha_h * \text{daily HTD base}_d (\text{°F}), \text{ where}$$

α_h , determined above, is a constant that is part of CT/home's thermal/HVAC heating run time model

daily HTD base_d is the baseline daily Heating Thermal Demand

d is the core heating day ($d = 001, 002, 003 \dots x$)

- CT heating savings is the percent heating run time reduction, for the reporting period in the CT input file.

$$\text{HS (\% RT reduction)} = 100 * \frac{(\text{RT base heat} - \text{RT actual heat})}{\text{RT base heat}}, \text{ where}$$

⁴ Thermostat module calls [Scipy Function leastsq to optimize](#), which uses [Levenberg-Marquardt](#) as implemented in MINPACK: LMDIF 1980

RT base heat is the sum of modeled baseline heating run times for all core heating days in the CT interval data file, and

RT actual heat is the sum of heating run times for all core heating days in the CT interval data file.

Assess Cooling Savings

- Develop the CT/home's unique thermal/HVAC cooling run time model
 - Calculate daily Cooling Thermal Demand (*daily CTD_d*) for each core cooling day in the interval data file:
 - Calculate the average hourly indoor minus outdoor temperature difference, expected to be negative (*hourly ΔT_{d,n}*), for each core heating day:
 - Using the ZIP code included in the metadata file, determine the closest NOAA weather station that is in the same climate zone as the CT and look up hourly outdoor temperatures:
 - hourly outdoor T_{d,n}*, where
 - d* is the core cooling day (*d* = 001, 002, 003 ... *x*),
 - n* is the hour; (*n* = 01, 02, 03, ... 24)
 - hourly ΔT_n (°F) = hourly indoor T_{d,n} - hourly outdoor T_{d,n}*, where
 - d* is the core heating day (*d* = 001, 002, 003 ... *x*), and
 - n* is the hour; (*n* = 01, 02, 03, ... 24)
 - Starting with an assumed value of zero for Tau ($\tau_c = 0$), calculate the daily Cooling Thermal Demand (*daily CTD_d*), as follows:
 - $$daily\ CTD_d(°F) = \frac{\sum_{n=1}^{24} [\tau_c - hourly\ \Delta T_{d,n}]_+}{24}$$
, where
 - d* is the core cooling day (*d* = 001, 002, 003 ... *x*),
 - n* is the hour; (*n* = 01, 02, 03, ... 24)
 - τ_c is the ΔT associated with $CTD = 0$ (zero cooling run time), reflecting that homes with no cooling running tend to be warmer than their surroundings, and
 - []₊ indicates that the term is zero if its value would be negative
 - For the set of all core cooling days in the CT interval data file, use ratio estimation to calculate α_c , the home's responsiveness to cooling, which should be positive
 - $$\alpha_c(\text{minutes}/°F) = \frac{RT\ actual\ cool}{\sum_{d=1}^x\ daily\ CTD_d}$$
, where
 - RT actual cool* is the sum of cooling run times for all core cooling days in the CT interval data file.
 - For the set of all core cooling days in the CT interval data file, optimize τ_c that results in minimization of the sum of squares of the difference between daily run times reported by the CT, and calculated daily cooling run times. Next recalculate α_c (iaw the above step) and record the model's parameters (τ_c , α_c)⁵:
 - $$\sum_{d=1}^x (actual\ RT\ cool_d - daily\ RT\ cool_d)^2$$
 is minimized, where
 - $daily\ RT\ cool_d = \alpha_c * daily\ CTD_d$
 - actual RT cool_d* is the total daily cooling run time reported by the CT for that core cooling day
 - d* is the core cooling day (*d* = 001, 002, 003 ... *x*)

Note that α_c characterizes the response of the home to cooling and τ_c is the difference between inside and outside temperatures when cooling run time = 0. Both are expected

⁵ Thermostat module calls [Scipy Function leastsq for optimization](#), which uses [Levenberg-Marquardt](#) as implemented in MINPACK: LMDIF 1980

to be positive.

- Calculate the cumulative baseline run time for the collection of all core cooling days in the CT interval data file (i.e. what would have occurred over the set of all core cooling days in the reporting period, had the home been held constant at the preferred cooling comfort temperature).
 - Calculate the baseline daily Cooling Thermal Demand (*daily CTD base_d*) for each core cooling day in the CT interval data file
 - Calculate the difference between the occupant's preferred comfort temperature for cooling and the average outside temperature for each hour of each core cooling day, expected to be negative (*hourly ΔT base cool_{d,n}*):

$$\text{hourly } \Delta T \text{ base}_n \text{ (}^\circ\text{F)} = T \text{ base cool} - \text{hourly outdoor } T_n$$
, where
 - d* is the core heating day (*d* = 001, 002, 003 ... *x*),
 - n* is the hour (*n* = 01, 02, 03, ... 24),
 - T base cool* is the occupant's preferred comfort temperature for cooling,
 - and
 - hourly outdoor T_n* is the average outdoor temperature for that hour reported by the nearest NOAA weather station in the same climate zone as the CT.
 - Calculate baseline daily Cooling Thermal Demand (*daily CTD base_d*)

$$\text{daily CTD base}_d = \frac{\sum_{n=1}^{24} [\tau_c - \text{hourly } \Delta T \text{ base cool}_{d,n}]_+}{24}$$
, where
 - d* is the core cooling day (*d* = 001, 002, 003 ... *x*),
 - n* is the hour (*n* = 01, 02, 03, ... 24),
 - τ_c , determined above, is a constant that is part of CT/home's thermal/HVAC cooling run time model, and
 - []₊ indicates that the term is zero if its value would be negative.
 - Calculate baseline run time as the sum of daily baseline run times for the set of core cooling days in the CT interval data file

$$\text{RT base heat (minutes)} = \sum_{d=1}^x \alpha_c * \text{daily CTD base}_d \text{ (}^\circ\text{F)}$$
, where
 - α_c , determined above, is a constant that is part of CT/home's thermal/HVAC cooling run time model
 - daily CTD base_d* is the baseline daily Cooling Thermal Demand
 - d* is the core cooling day (*d* = 001, 002, 003 ... *x*)
 - CT cooling savings is the percent cooling run time reduction for the reporting period in the CT input file.

$$CS(\% \text{ RT reduction}) = 100 * \frac{(\text{RT base cool} - \text{RT actual cool})}{\text{RT base cool}}$$
, where

RT base cool is the sum of calculated baseline cooling run times for all core cooling days in the CT interval data file, and

RT actual cool is the sum of cooling run times for all core cooling days in the CT interval data file.

Calculate RU

- Resistance Heating Utilization (RU) – for heat pump systems only, calculate RU in 12 (daily average) outdoor temperature bins (0 ≤ T < 5°F, 5 ≤ T < 10°F, ..., 55 ≤ T ≤ 60°F). For example RU_{0-5F} is calculated as follows:

$$RU_{0-5F} = \frac{(t_{emerg_{0-5F}} + t_{aux_{0-5F}})}{(t_{emerg_{0-5F}} + t_{comp_{0-5F}})}$$

where,

$t_{emerg_{0-5F}}$ = total emergency resistance heating run time in the interval data file that occurs on core heating days where $0^{\circ}\text{F} \leq$ average daily outdoor temperature $< 5^{\circ}\text{F}$. t_{emerg} is in lieu of compressor operation, e.g. use of electric resistance strip heat under fault conditions or when the outside temperature is very low,

$t_{aux_{0-5F}}$ = total annual auxiliary resistance heating run time in the interval data file that occurs on core heating days where $0^{\circ}\text{F} \leq$ average daily outdoor temperature $< 5^{\circ}\text{F}$. t_{aux} is supplemental to compressor operation, e.g. use of electric resistance strip heat to increase heating capacity, and

$t_{comp_{0-5F}}$ = total compressor heating run time in the interval data file that occurs on core heating days where $0^{\circ}\text{F} \leq$ average daily outdoor temperature $< 5^{\circ}\text{F}$. A proportion of t_{comp} may occur when auxiliary resistance heating also occurs.

STATISTICS MODULE IMPLEMENTATION DETAIL

After the thermostat module generates an output file for the sample set, the statistics module leverages these files to assess average savings, expressed as percent run time reduction.

- Assess average heating savings, cooling savings, and RU for each of the five EIA climate zones, for example

$\text{CT Savings}_{\text{heat Mixed-Humid}} = \sum \text{CT}_i \text{ Savings}_{\text{heat Mixed-Humid}} / n$, where

$i = 1$ thru n , and

n = the number of CTs in the EIA Mixed-Humid climate region

- Nationally – from regional savings, national savings are calculated as weighted averages for heating and cooling. (see below for details on Climate Zone weightings). Statistics associated with nationally weighted savings estimates include the mean, standard error of the mean, decile bins (q10-q90) and the Lower Bound of the 95th Percentile Confidence Interval (LB95). The Nationally Weighted LB95 is calculated via the following formula:

$$SE_{\text{National}} = \sqrt{\sum_{\text{CZ}=1}^5 (W_{\text{CZ}} * SE_{\text{CZ}})^2}$$

Where SE_{CZ} are the standard errors in each climate zone, calculated as the standard deviation in the climate zone divided by the square root of the number of CTs analyzed in that climate zone, W_{CZ} are the climate zone weightings, and SE_{National} is the standard error of the weighted mean.

The Nationally Weighted LB95 is calculated from the SE_{National} via the following:

$$LB95_{\text{National}} = \text{Mean}_{\text{National}} - 1.96 * SE_{\text{National}}$$

Key performance metrics, Nationally Weighted LB95 and 20th decile bin q20 are specifically labelled and placed in the output file for ease of reference.

- Weighting for heating and cooling is by the proportion of national heating or cooling energy used in each of the five EIA climate zones, as follows:

Heating	
<i>Climate Region</i>	<i>%BTU vs National</i>
Very Cold/Cold	54.9%
Mixed-Humid	31.2%
Mixed-Dry/Hot-Dry	5.4%
Hot-Humid	4.9%
Marine	3.6%

Cooling	
<i>Climate Region</i>	<i>%BTU vs National</i>
Very Cold/Cold	9.6%
Mixed-Humid	34.0%
Mixed-Dry/Hot-Dry	14.4%
Hot-Humid	42.0%
Marine	Not included

- All other National outputs, including National RHU, are calculated as an unweighted average over all CTs in the sample set.